

OXFORD CAMBRIDGE AND RSA EXAMINATIONS
GCSE

J567/04

MATHEMATICS B

Paper 4 (Higher Tier)

FRIDAY 8 NOVEMBER 2013: Morning

**DURATION: 1 hour 45 minutes
plus your additional time allowance**

MODIFIED ENLARGED

Candidate forename		Candidate surname	
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Centre number						Candidate number				
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Candidates answer on the Question Paper.

OCR SUPPLIED MATERIALS:

None

OTHER MATERIALS REQUIRED:

**Geometrical instruments
Tracing paper (optional)
Scientific or graphical calculator**

<p>YOU ARE PERMITTED TO USE A CALCULATOR FOR THIS PAPER</p>
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READ INSTRUCTIONS OVERLEAF

INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the boxes on the first page. Please write clearly and in capital letters.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer ALL the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Your answers should be supported with appropriate working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).

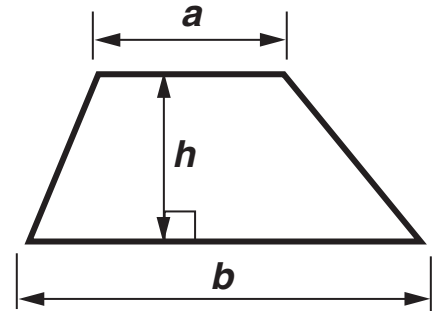
INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.
- Your quality of written communication is assessed in questions marked with an asterisk (*).
- The total number of marks for this paper is 100.

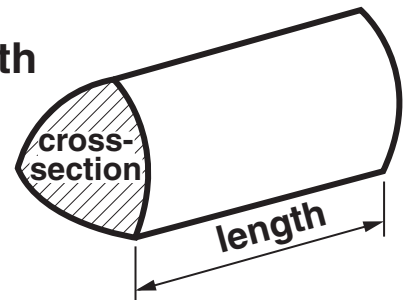
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FORMULAE SHEET: HIGHER TIER

Area of trapezium = $\frac{1}{2}(a + b)h$



Volume of prism = (area of cross-section) \times length

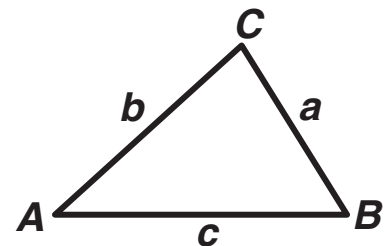


In any triangle *ABC*

Sine rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

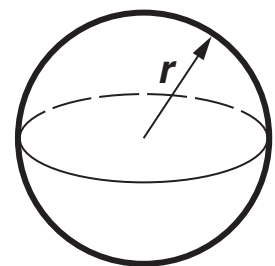
Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle = $\frac{1}{2}ab \sin C$



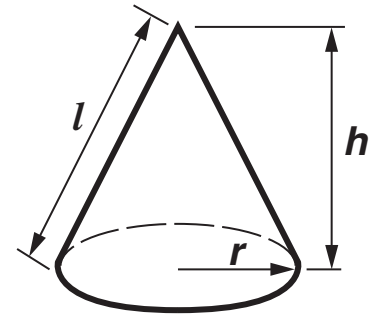
Volume of sphere = $\frac{4}{3}\pi r^3$

Surface area of sphere = $4\pi r^2$



Volume of cone = $\frac{1}{3}\pi r^2 h$

Curved surface area of cone = $\pi r l$



The Quadratic Equation

**The solutions of $ax^2 + bx + c = 0$,
where $a \neq 0$, are given by**

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

Answer ALL the questions.

1 (a) Calculate.

$$\frac{6.3^2 - 3.7}{5.8}$$

Write your answer correct to 2 decimal places.

(a) _____ [2]

(b) Calculate.

$$\sqrt{4.5 \times 6.7 + 1.8 \times 2.4}$$

Write your answer correct to 2 significant figures.

(b) _____ [2]

- 2 Samuel has six types of coin in a bag.
The following table shows the probability of each type of coin being picked.**

Coin	1p	2p	5p	10p	20p	50p
Probability	0.07	0.23	0.18	0.28	0.19	x

(a) Work out x .

(a) _____ [2]

(b) Samuel picks one coin out of the bag at random.

Work out the probability that he picks a coin worth 5p or less.

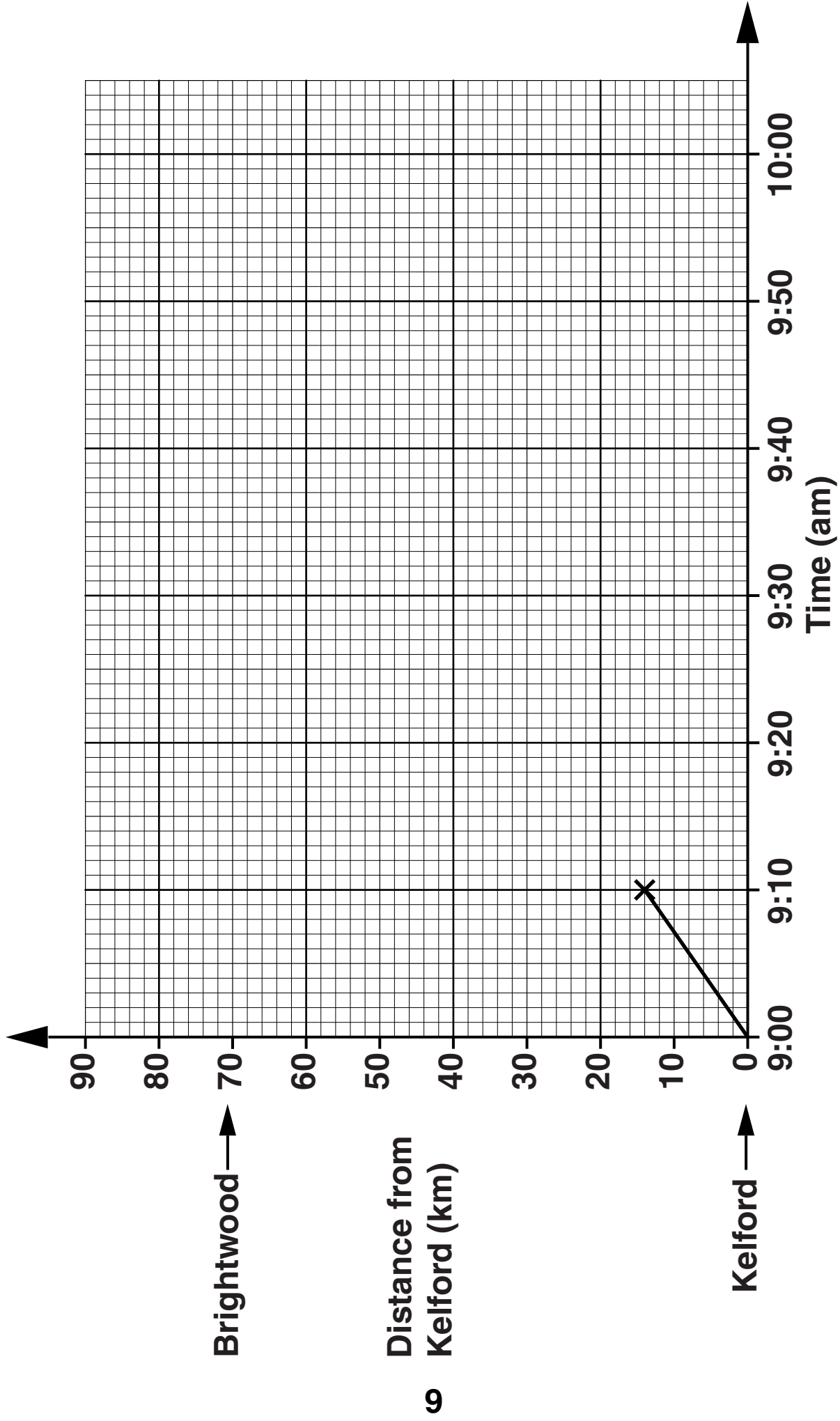
(b) _____ [2]

**3 A train travels from Kelford to Brightwood.
The graph opposite shows the first ten minutes of the
train's journey.**

**The two stations are 70 kilometres apart.
The train is due to arrive at Brightwood at 10:00 am.**

**Will it arrive on time if it continues to travel at the
same speed?
Show clearly how you decide.**

[3]



4 (a) Here are the first four terms of a sequence.

7 12 17 22

Write an expression for the n th term of this sequence.

(a) _____ [2]

(b) The n th term of another sequence is given by the expression $100 - 8n$.

Write down the first three terms of this sequence.

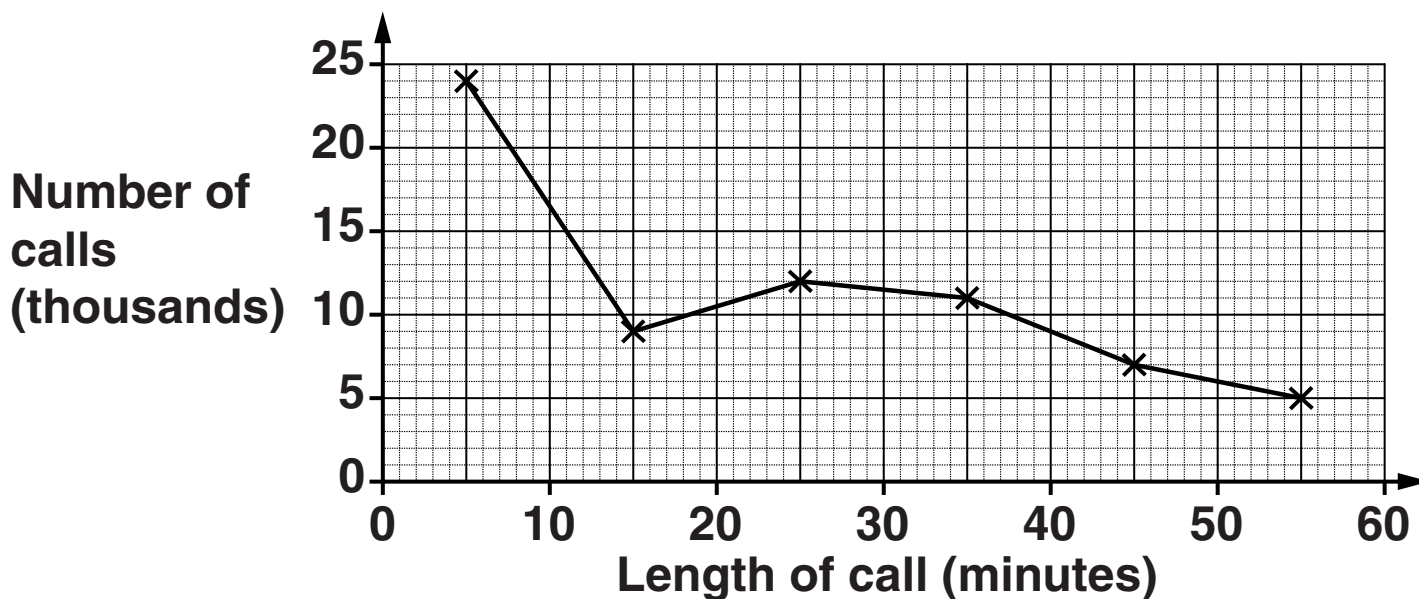
(b) _____ , _____ , _____ [2]

5 Solve.

$$6(2x - 3) = 24$$

x = _____ [3]

- 6 (a) The Bilberry Telephone Company records the lengths of telephone calls in one day. The information is summarised in the frequency polygon below.



- (i) Estimate how many calls lasted less than 20 minutes.

(a)(i) _____ thousand [2]

- (ii) Write down the modal class.

(ii) _____ minutes [1]

(b) The lengths of Desmond's telephone calls, in minutes, are summarised in the table below.

Length of call (t minutes)	Number of calls		
$0 < t \leq 10$	0		
$10 < t \leq 20$	3		
$20 < t \leq 30$	3		
$30 < t \leq 40$	6		
$40 < t \leq 50$	8		
$50 < t \leq 60$	5		

Calculate an estimate of the mean length of Desmond's calls.

(b) _____ minutes [4]

- (c) The table below summarises the lengths, in minutes, of Harriet's calls in November and December.

	Mean	Range
November	34.2	67.4
December	39.7	43.8

- (i) In which month were Harriet's calls longer on average?

Explain how you decide.

[1]

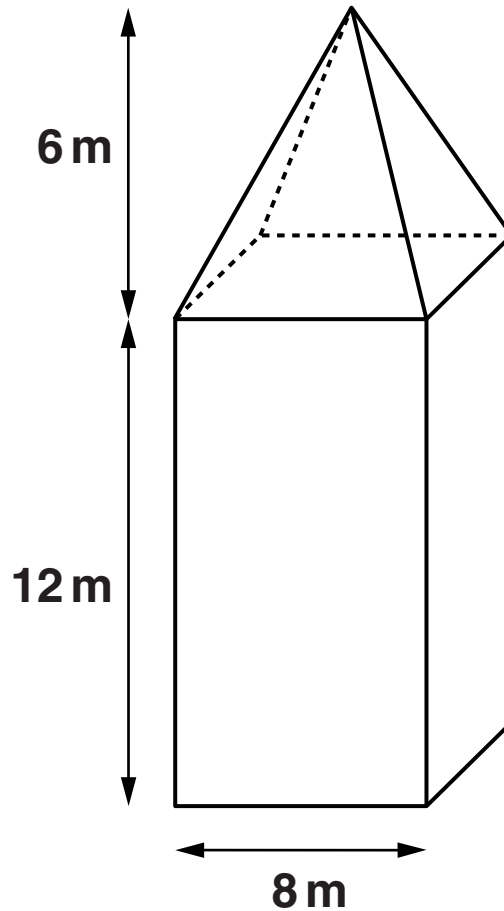
- (ii) In which month were the lengths of Harriet's calls more spread out?

Explain how you decide.

[1]

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- 7 A tower is in the shape of a cuboid with a pyramid on top.
The height of the cuboid is 12 m and the height of the pyramid is 6 m.
The base of the tower is a square of side 8 m and it has a TOTAL height of 18 m.

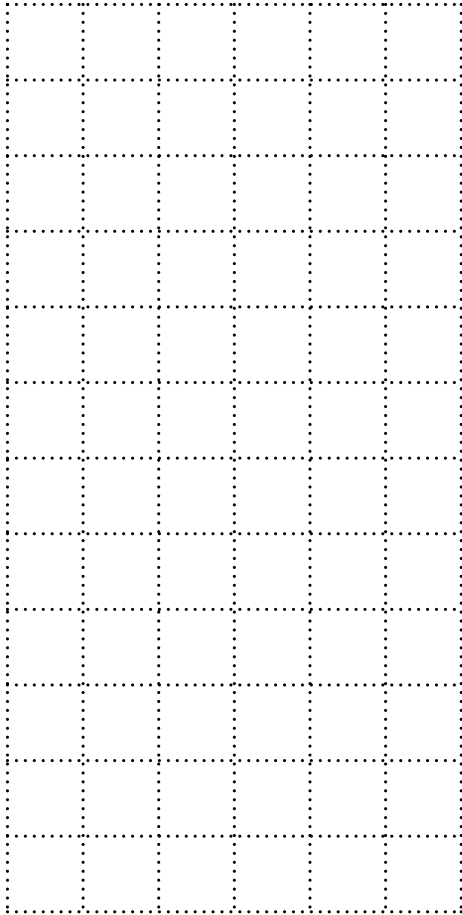


**On the grids below draw accurately the plan and the front elevation of the tower.
Use a scale of 1 cm to 2 m. [4]**

Plan



Front Elevation



- 8 (a) Riverside Tennis Club has 24 members.
They have four types of membership.

SM Senior Male
SF Senior Female
JM Junior Male
JF Junior Female

The membership information is recorded below.

SM	JM	SM	JM	SF	JM	SM	JF
JM	SF	JF	SM	SM	JF	SF	SM
SF	SM	JM	JM	JF	SM	JM	SF

- (i) On the grid below, design and draw a two-way table to show this information. [3]

(ii) One member is selected at random.

Write down the probability that the member is a Junior.

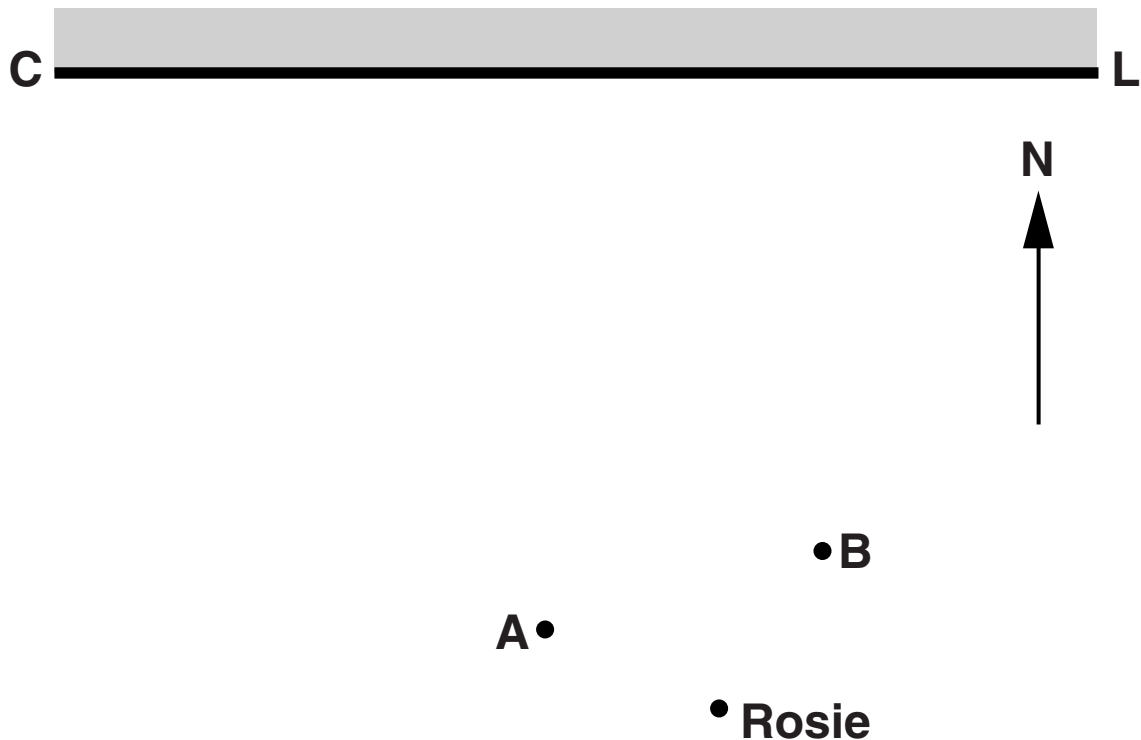
(a)(ii) _____ [1]

(b) In 2011, Greenmeadows Tennis Club had 25 members and in 2012 it had 31 members.

Calculate the percentage increase in the number of members.

(b) _____ % [3]

- 9 The scale diagram below shows a coastline, CL.
A and B are two rocks in the sea.
The scale of the diagram is 1 cm represents 500 m.



SCALE: 1 cm REPRESENTS 500 m

Rosie is sailing her boat.

She sails on a course towards the coast so that she is an equal distance from the rocks, A and B.

When she is less than 1 km from the coast she turns and sails due West.

She now sails so that she is between 500 m and 1 km from the coast.

Construct a route that Rosie could take.

You must leave in all your construction lines. [4]

**10 Gwen is taking her class of 28 pupils to a pantomime.
The total cost of the trip is £575.**

**Use estimation to find an approximate cost of this trip
for each pupil.**

Show your working clearly.

$$\underline{\hspace{10em}} \div \underline{\hspace{10em}} = \underline{\hspace{10em}} \quad [2]$$

11 Here are six equations of straight lines, each labelled with a letter.

A

$$y = 4x - 7$$

B

$$y = 3x + 14$$

C

$$y = 2x + 5$$

D

$$y = -3x + 1$$

E

$$y = 14x - 7$$

F

$$y = 4x + 3$$

Choose the correct letters to make each statement true. [3]

Line _____ is the steepest line.

Lines _____ and _____ are parallel.

Lines _____ and _____ meet on the y -axis.

12 In Westercote, house prices rose by 6% from 2010 to 2011.

(a) On 1 January 2010 a house was priced at £180 000.

Calculate its price on 1 January 2011.

(a) £ _____ [3]

(b) On 1 January 2011 another house was priced at £371 000.

Calculate its price on 1 January 2010.

(b) £ _____ [3]

13 (a) Multiply out and simplify.

$$(x + 7)(x - 3)$$

(a) _____ [2]

(b) Factorise fully.

$$6xy - 12x^2$$

(b) _____ [2]

(c) Rearrange this formula to make x the subject.

$$A = x^2 - 4y$$

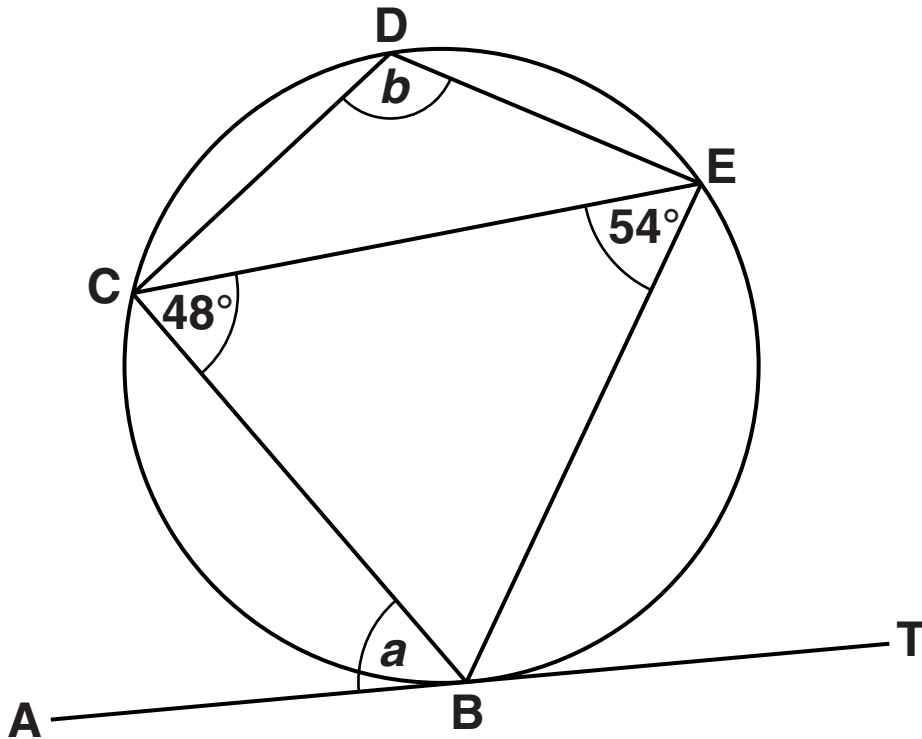
(c) _____ [2]

(d) y is inversely proportional to x and $y = 30$ when $x = 4$.

Write an equation linking x and y .

(d) _____ [3]

- 14 In the diagram below B, C, D and E are points on the circumference of a circle.
 AT is the tangent to the circle at B.
 Angle BCE = 48° and angle BEC = 54° .



NOT TO SCALE

- (a) Find angle a .
 Give a reason for your answer.

(a) Angle $a =$ _____ $^\circ$

[2]

- (b) Calculate angle b .
Give a reason for each step of your working.**

(b) Angle $b =$ _____ $^{\circ}$ [3]

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15 A town has a population of 120 000, correct to the nearest ten thousand, and an area of 54 km², correct to the nearest whole number.

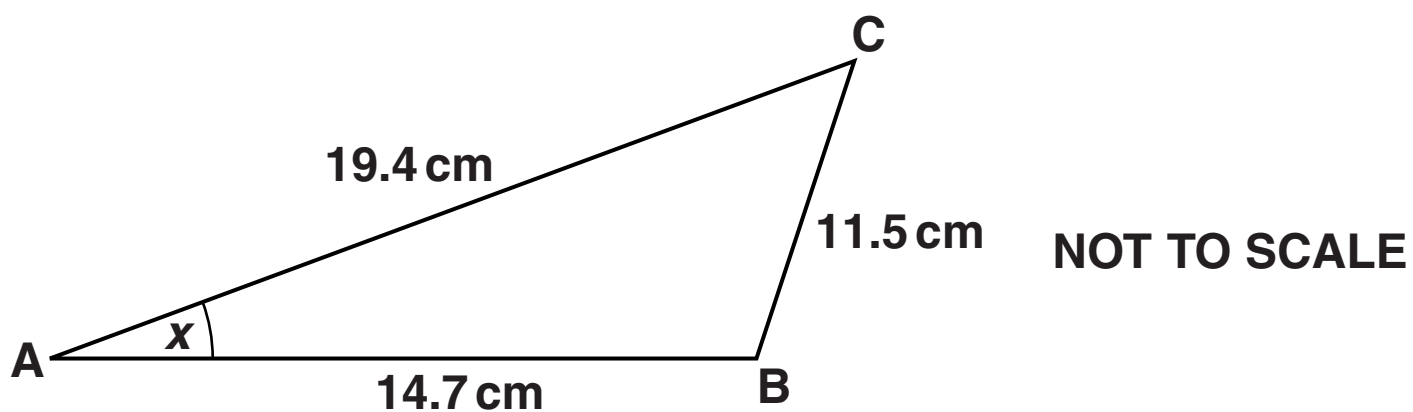
(a) Write down the upper bound of the population.

(a) _____ [1]

(b) Calculate the upper bound of the population density.

(b) _____ people/km² [3]

- 16 (a) The diagram below shows a triangle ABC.
AB = 14.7 cm, BC = 11.5 cm and AC = 19.4 cm.

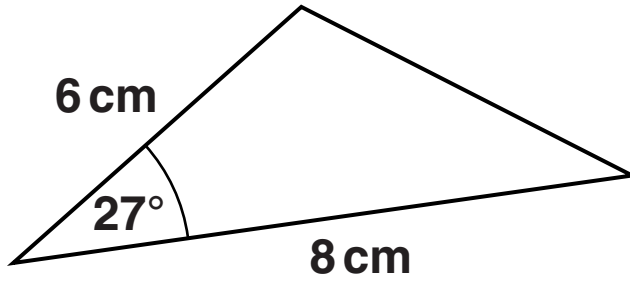


- (i) Show that triangle ABC is NOT a right-angled triangle. [3]

(ii) Calculate angle x.

(a)(ii) _____ ° [3]

(b) Calculate the area of this triangle.



NOT TO SCALE

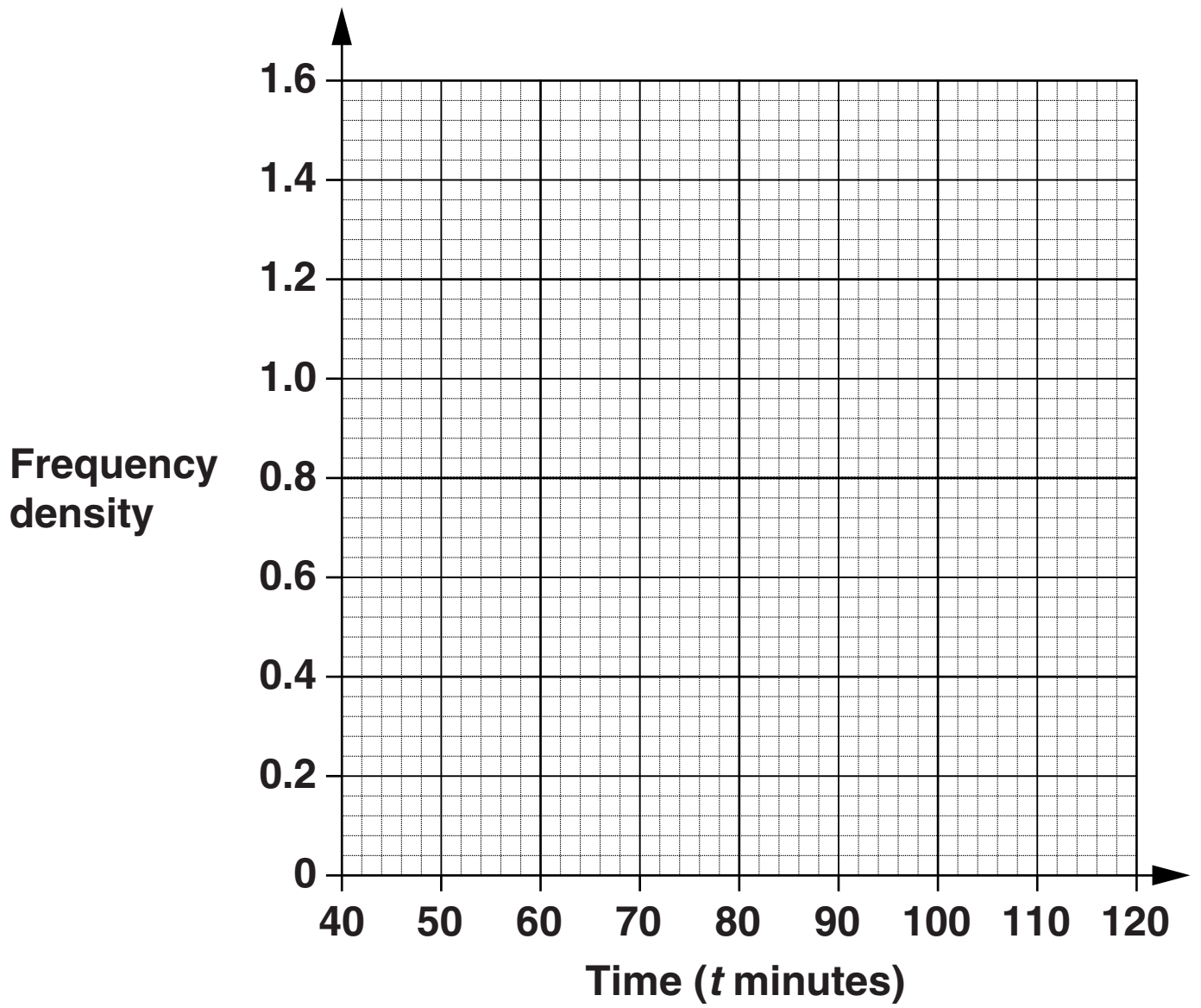
(b) _____ cm² [2]

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- 17** A teacher records the times taken for pupils to complete a cross-country course.
The results are summarised in the table below.

Time (t minutes)	Number of pupils
$40 < t \leq 50$	8
$50 < t \leq 60$	15
$60 < t \leq 80$	6
$80 < t \leq 120$	4

Draw a histogram on the grid opposite to show this data. [3]



18 (a) Solve algebraically.

$$5x - 2y = 22$$

$$2x + 3y = 5$$

(a) $x =$ _____

$y =$ _____ **[4]**

(b) (i) Write $x^2 - 6x + 4$ in the form $(x + a)^2 + b$.

(b)(i) _____ [3]

**(ii) Using your answer to (b)(i), or otherwise,
solve $x^2 - 6x + 4 = 0$.
Write your answers correct to 1 decimal place.**

(ii) $x =$ _____ or $x =$ _____ [2]

**19 On Finch Island there are bullfinches and chaffinches.
In the spring of 2013:**

**the population of bullfinches was 6700 and was
DECREASING by 3% each year,**

**the population of chaffinches was 4800 and was
INCREASING by 4% each year.**

**In the spring of which year will the population
of chaffinches first be greater than that of the
bullfinches?**

Show your working clearly.

[4]

20* Assume that the Earth is a sphere with radius 6371 km.
The land area on the surface of the Earth is 148 940 000 km².

Use this information to show that the ratio of land area to water area is approximately 3 : 7.

[5]

END OF QUESTION PAPER

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