## GCSE

## Mathematics B (Linear)

General Certificate of Secondary Education

## Mark Scheme for November 2013

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, OCR Nationals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

Annotations used in the detailed Mark Scheme.

| Annotation | Meaning |
| :---: | :---: |
| $\checkmark$ | Correct |
| $\stackrel{3}{ }$ | Incorrect |
| BOD | Benefit of doubt |
| FT | Follow through |
| 15w | Ignore subsequent working (after correct answer obtained), provided method has been completed |
| M0 | Method mark awarded 0 |
| M11 | Method mark awarded 1 |
| M2 | Method mark awarded 2 |
| A1 | Accuracy mark awarded 1 |
| B1 | Independent mark awarded 1 |
| B2 | Independent mark awarded 2 |
| MR | Misread |
| SC | Special case |
| $\wedge$ | Omission sign |

These should be used whenever appropriate during your marking.
The M, A, B, etc annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate these scripts to show how the marks have been awarded.
It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

## Subject-Specific Marking Instructions

1. $\mathbf{M}$ marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding $\mathbf{M}$ (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage. SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, eg FT $180 \times$ (their ' $37{ }^{\prime}+16$ ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2}$ ). Answers to part questions which are being followed through are indicated by eg FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $x$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) | (i) | $2^{5} \times 3$ <br> Or $2 \times 2 \times 2 \times 2 \times 2 \times 3$ or better | 2 | M1 for correct factor pair or product seen or attempt at factor tree/ladder with at least two steps or answer $2^{k} \times 3$ oe OR <br> SC1 for 2, 2, 2, 2, 2, 3 identified but not as product | Condone $3^{1}$ for 2 or 1 marks May be part of factor tree or eg $4 \times 8 \times 3$ May contain errors |
|  |  | (ii) | 12 final answer | 2 | B1 for 2, 2, 3 clearly identified for both 96 and 108 or answer of $2,3,4$ or 6 oe | e.g. in a Venn diagram e.g. accept $2^{2}$ for B1 |
|  | (b) |  | $5 \frac{1}{6}$ final answer | 3 | B2 for $5 \frac{2}{12}$ or $\frac{62}{12}$ seen or other unsimplified equivalent OR <br> M1 for $1 \frac{3}{4}$ converted to $1 \frac{9}{12}$ or $\frac{21}{12}$ <br> AND <br> M1 for correct addition of their two improper fractions/mixed numbers with common denominator AND <br> M1 for their improper fraction/mixed number correctly converted to a mixed number in its lowest terms max 2 marks if answer incorrect | M1 may be implied by $\frac{3}{4}$ converted to $\frac{9}{12}$ but not $3 \frac{9}{12}$ Or M1 for other conversion to common denominator with at least one correct numerator <br> allow this M1 even if no simplification required |
| 2 | (a) |  | $\begin{aligned} & -7 \\ & 125 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  |  |


| Question |  |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) |  | 21 | 2 | M1 for 9 from $b^{2}$ or +3 from $-b$ soi Or for $2 \times(-3)^{2}--3$ seen | e.g. $-36--3=-33$ implies M1 Condone missing brackets in $(-3)^{2}$ if result 9 seen |
| 3 | (a) |  | 97.28 [p] | 4 | B3 for 24.32 seen from $12.8 \times 1.9$ or answer $£ 97.28$ or figs 9728 <br> OR <br> M1 for $1.9 \times 4 \times 12.8$ soi <br> AND <br> B1 for figs 76, 512, 38, 152, 1152 $896,768,608,4608$ or 95 seen <br> AND <br> B1 for answer in range 87 to 104 | allow rounding of 97.28 seen for 4 marks <br> May be seen in stages, may be done in any order but not using rounded values. Condone additional multiplication by 7 |
|  | (b) | (i) | 4 9        <br> 5 3 4 7      <br> 6 0 4 7 8     <br> 7 0 3 3 4 4 7 8  <br> 8 6        | 3 | M2 for table with 4 correct rows Or <br> M1 for unordered diagram with at most one error or omission |  |




| Question |  |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | (a) | (i) | $\frac{74}{120} \text { oe }$ | 1 | accept $0.616[\ldots]$ or 0.617 <br> or $61.6[\ldots][\%]$ or $61.7 \%$ or better | do not accept ratio as answer <br> isw for incorrect cancelling or 74 in 120 or 74 out of 120 etc after correct fraction seen Condone 'likely' after correct fraction seen |
|  |  | (ii) | 600 final answer | 2 | M1 for $\frac{30}{120} \times 2400$ oe or for 600 seen with 2400 | e.g. $\frac{600}{2400}$ or 600 out of 2400 |
|  | (b) |  | 50 | 2 | $\text { M1 for } \frac{1500}{2400} \times 80 \text { oe }$ |  |
| 6 | (a) |  | $x \leq 4$ | 2 | M1 for $3 x \leq 8+4$ or better AND <br> M1 for $x \leq \frac{b}{a}$ after $a x \leq b$ seen max 1 mark if answer incorrect OR <br> SC1 for answer 4 or $x \ldots 4$ with any incorrect equality or inequality symbol or answer $3 \times 4-4 \leq 8$ | Condone use of = or incorrect inequality symbol in place of $\leq$ for all method marks $a \neq 1, b \neq 0$ <br> condone e.g. '4 or less' as answer for SC1 |
|  | (b) |  |  | 1 | FT their inequality in (i) | Condone any indication at 4 Condone missing arrow at other end but do not accept indication of the line terminating Accept any length line |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 |  | Use of $360^{\circ}$ at point Or use of symmetry to halve $90^{\circ}$ <br> [Angle in each polygon $=$ ] $135\left[{ }^{\circ}\right.$ ] <br> Number of sides $=360 \div(180-$ their 135$)$ <br> Octagon | B1 <br> B1 <br> B1 <br> B1 | e.g. $360-90$ seen or angles summing to 360 seen or exterior angle is 45 <br> or identifying polygon has 8 sides or $180(n-2)=135 n$ used | implied by 270 seen <br> condone poor notation for division e.g. $45 \div 360$ if intention clear <br> All marks independent |
| 8 | (a) | Triangle B correctly positioned Vertices (-4, -2), (-4, -3), (-1, -2) | 4 | B3 for triangle B with two vertices correct <br> Or for correct rotation followed by translation by 5 left or 1 down <br> Or for correct translation following $90^{\circ}$ anticlockwise rotation about origin OR <br> B2 for correct rotation of A clockwise about origin followed by incorrect or no translation <br> Or for $90^{\circ}$ anticlockwise rotation about origin followed by translation by 5 left or 1 down <br> OR <br> B1 for rotation of $\mathrm{A} 90^{\circ}$ anticlockwise about origin followed by incorrect or no translation <br> OR <br> SC2 for correct translation following $180^{\circ}$ rotation about origin OR <br> SC1 for translation of 5 left or 1 down following $180^{\circ}$ rotation about origin | Use overlay <br> Accept intention if triangles not labelled <br> Red triangle scores 4 marks, horizontal or vertical translation of red scores B3, any other translation of red scores B2 <br> Green triangle scores B3, horizontal or vertical translation of green scores B2, any other translation of green scores B1 <br> Blue triangle scores SC2, horizontal or vertical translation of blue scores SC1, any other translation of blue scores SC0 |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | [Centre] ( ${ }^{-1}, 2$ ) and [scale factor] ${ }^{-2}$ with no other transformation | 2 | $\begin{aligned} & \text { B1 for }(-1,2) \\ & \text { Or } \\ & \text { B1 for }{ }^{-2} \end{aligned}$ | Do not accept centre written as vector Condone e.g. 'negative enlargement of 2' for scale factor ${ }^{-2}$ |
| 9 |  | [Shortest side = ] 7 nfww | 5 | M4 for $x=4$ nfww <br> OR <br> M1 for $8 x+2$ or $4 x+18$ seen <br> AND <br> M1 for their ' $8 x+2$ ' $=$ their ' $4 x+18$ ' <br> AND <br> M1 for correctly collecting terms their ' $8 x-4 x^{\prime}=$ their ' $18-2$ ' <br> AND <br> M1 for $x=\frac{b}{a}$ after $a x=b$ seen <br> AND <br> M1 for correctly evaluating $11-x$ using their positive $x$ <br> max 4 marks if answer incorrect | allow 5 marks for $11-x$ on answer line if seen evaluated as 7 in working <br> accept unsimplified <br> any equivalent equation $\mathbf{F T}$ their attempts at perimeters <br> FT their linear equation <br> $a \neq 1$ and $a \neq b$ and $\frac{b}{a}>0$ $0<x<11$ <br> Trial and improvement methods can score 5 for shortest side $=7$ or 4 for $x=4$ only. Answer 7 with no working scores 5 |
| 10 | (a) | $\begin{array}{lllll}5 & 15 & 34 & 48 & 60\end{array}$ | 1 |  |  |


| Question |  | Answer | Marks | Part Marks and Guidance |
| :--- | :--- | :--- | :---: | :--- | :--- | :--- |
| (b) | $\begin{array}{l}\text { All points plotted correctly and joined with } \\ \text { smooth curve or straight line segments }\end{array}$ | 2 | $\begin{array}{l}\text { FT their table } \\ \text { B1 for at least 4 points plotted at } \\ \text { correct height within interval }\end{array}$ | $\begin{array}{l}\text { Allow } \pm 1 \text { mm for plotting points } \\ \text { and drawing curve, use overlay } \\ \text { for guidance } \\ \text { Condone starting at (20, 5) }\end{array}$ |
| Mark curve generously |  |  |  |  |
| Bar chart only scores 0, bar |  |  |  |  |
| chart with curve scores max |  |  |  |  |
| B1 |  |  |  |  |$]$


| Question |  |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (a) | (i) | 1.8 | 2 | M1 for $3 \times 0.6$ or answer figs 18 |  |
|  |  | (ii) | 1800 | 1FT | FT $1000 \times$ their 1.8 | strict follow through |
|  | (b) | (i) | $0.03\left[\mathrm{~m}^{2}\right]$ | 3 | M2 for $0.1^{2}$ soi Or <br> M1 for 100 seen or scale factor 0.1 soi | accept answer $300 \mathrm{~cm}^{2}$ if units clearly stated <br> e.g. M1 implied by answer 0.3 |
|  |  | (ii) | 1.8 | 1FT | FT their (a)(ii) $\div 1000$ | strict follow through |
| 13 |  |  | Correct region R indicated | 3 | B2 for region on the correct side of two inequalities <br> B1 for region on the correct side of one inequality | Do not assume axes are boundaries unless identified by shading i.e. if no shading, assume that the region is bounded by the inequality lines If no label $R$, assume shading identifies region unless clearly shading out each individual inequality <br> If their region is bounded by lines other than those given maximum B1 may be awarded |
| 14 |  |  |   | 2 | both correct, first line any with positive gradient, second line any with negative gradient or horizontal or vertical line <br> both correct, first graph any with two positive solutions, second any with one/no positive solutions Or <br> B1 for any one parabola seen | accept any clear intention of correct graphs, ie not ruled but attempt at straight line <br> Accept any clear intention of correct graphs, ie attempt at parabola <br> Condone more than one parabola on axes for B1 |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 |  | $\frac{5}{8} \text { oe }$ | 4 | M3 for sum of at least four of required probabilities seen: DD, DM, MD, DW and WD <br> Or for $P(D)+P(M D)+P(W D)$ <br> Or for 1 - P (no dark) <br> OR <br> M2 for $\mathrm{P}($ no dark $)=\frac{10}{16} \times \frac{9}{15}$ or $\frac{3}{8}$ <br> Or for correct tree diagram showing probabilities on sufficient branches Or for at least two of the five required probabilities found <br> OR <br> M1 for at least one correct combined probability seen <br> Or for three correct probabilities for first chocolate seen: $M=\frac{8}{16}, D=\frac{6}{16} \text { and } W=\frac{2}{16}$ <br> Or for identifying the five required pairs of outcomes: DD, DM, MD, DW and WD <br> OR <br> SC2 for answer $\frac{27}{28}$ or $\frac{39}{64}$ Or <br> SC1 for correct tree diagram assuming just 6 dark, 2 white chocolates or correct tree diagram assuming replacement | allow all method marks if correct multiplication seen, even if not evaluated or incorrectly evaluated $\begin{aligned} & P(M M)=\frac{8}{16} \times \frac{7}{15}=\frac{7}{30} \\ & P(M D)=\frac{8}{16} \times \frac{6}{15}=\frac{1}{5} \\ & P(M W)=\frac{8}{16} \times \frac{2}{15}=\frac{1}{15} \\ & P(D M)=\frac{6}{16} \times \frac{8}{15}=\frac{1}{5} \\ & P(D D)=\frac{6}{16} \times \frac{5}{15}=\frac{1}{8} \\ & P(D W)=\frac{6}{16} \times \frac{2}{15}=\frac{1}{20} \\ & P(W M)=\frac{2}{16} \times \frac{8}{15}=\frac{1}{15} \\ & P(W D)=\frac{2}{16} \times \frac{6}{15}=\frac{1}{20} \\ & P(W W)=\frac{2}{16} \times \frac{1}{15}=\frac{1}{120} \end{aligned}$ <br> allow equivalent marks throughout for methods using dark/not dark |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | (a) | 4.5 | 3 | nfww <br> M1 for eliminating fraction and expanding bracket $3 x-1=5 x-10$ <br> AND <br> M1 for collecting terms FT $-1+10=5 x-3 x$ <br> AND <br> M1 for $x=\frac{b}{a}$ after $a x=b$ seen max 2 marks if answer incorrect | condone $3 x-1=5 x-2$ <br> or $3 x-1=x-10$ <br> or $0.6 x-0.2=x-2$ for M1 <br> correct collection from $a x+b=$ $c x+d$ to $a x-c x=d-b$ <br> $a \neq 1$ or 0 and $a \neq b$ and $b \neq 0$ |
|  | (b) | $a^{8}$ | 2 | M1 for $\left(a^{-4}\right)^{-2}$ or $\left(\frac{1}{a^{4}}\right)^{-2}$ or $\left(\frac{a^{9}}{a^{5}}\right)^{2}$ or $\frac{a^{-10}}{a^{-18}}$ or $\frac{a^{18}}{a^{10}}$ seen | condone $a^{-4-2}$ for M1 |
|  | (c) | $\frac{14-x}{(x-2)(x+1)} \text { or } \frac{14-x}{x^{2}-x-2}$ | 3 | M1 for $4(x+1)-5(x-2)$ <br> or $4 x+4-5 x+10$ with three terms correct or better seen <br> M1 for correct common denominator seen as denominator | Mark final answer but isw for incorrect expansion of denominator after correct denominator seen May be in two separate fractions <br> condone missing final bracket in denominator |
| 17 | (a) | $\mathbf{a + b}$ final answer | 1 |  |  |
|  | (b) | b-a final answer | 1 |  | Condone $\mathbf{b}+\mathbf{-} \mathbf{a}$ |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (c) | $\frac{1}{3}(\mathbf{a}+\mathbf{b})$ or $\frac{1}{3} \mathbf{a}+\frac{1}{3} \mathbf{b}$ final answer | 1 | $\text { FT } \frac{1}{3}\left(\text { their }^{\prime} \mathbf{a}+\mathbf{b}^{\prime}\right)$ |  |
|  | (d) | $\frac{1}{3}(2 \mathbf{b}-\mathbf{a})$ or $\frac{2}{3} \mathbf{b}-\frac{1}{3} \mathbf{a}$ final answer | 2 | M1 for $-\frac{1}{3}(\mathbf{a}+\mathbf{b})+\mathbf{b}$ oe or for $\mathbf{b} \pm$ their ${ }^{\frac{1}{3}}(\mathbf{a}+\mathbf{b})^{\prime}$ or for $\overrightarrow{X O}+\overrightarrow{O R}$ or $\overrightarrow{X Q}+\overrightarrow{Q R}$ soi |  |
| 18 |  | $20+5 \sqrt{3}$ | 4 | B1 for $\sqrt{5}$ or $\sqrt{15}$ or $\sqrt{75}$ seen <br> M1 for $\left[\frac{1}{2} \times\right] \sqrt{5} \times \sqrt{15}$ <br> M1 for total area $=15+5+2 \times \frac{1}{2} \times \sqrt{5} \times \sqrt{15} \text { or }$ <br> better <br> M1 for $5 \sqrt{3}$ seen max 3 marks if answer incorrect | $\sqrt{75}$ seen implies B1 and M1 <br> may be implied by adding their 'simplified' $\sqrt{5} \times \sqrt{15}$ to 20 |



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